Question Number : 1

The product of eigenvalues of the matrix \( P \) is

\[
P = \begin{bmatrix}
  2 & 0 & 1 \\
  4 & -3 & 3 \\
  0 & 2 & -1
\end{bmatrix}
\]

(A) \(-6\) \hspace{1cm} (B) \(2\) \hspace{1cm} (C) \(6\) \hspace{1cm} (D) \(-2\)

Correct : 1  Wrong : -0.33

Question Number : 2

The value of \( \lim_{x \to 0} \frac{x^3 - \sin(x)}{x} \) is

(A) \(0\) \hspace{1cm} (B) \(3\) \hspace{1cm} (C) \(1\) \hspace{1cm} (D) \(-1\)

Correct : 1  Wrong : -0.33

Question Number : 3

Consider the following partial differential equation for \( u(x, y) \) with the constant \( c > 1 \):

\[
\frac{\partial u}{\partial y} + c \frac{\partial u}{\partial x} = 0
\]

Solution of this equation is

(A) \( u(x, y) = f(x + cy) \) \hspace{1cm} (B) \( u(x, y) = f(x - cy) \)

(C) \( u(x, y) = f(cx + y) \) \hspace{1cm} (D) \( u(x, y) = f(cx - y) \)

Correct : 1  Wrong : -0.33

Question Number : 4

The differential equation \( \frac{d^2 y}{dx^2} + 16y = 0 \) for \( y(x) \) with the two boundary conditions \( \frac{dy}{dx} \bigg|_{x=0} = 1 \) and \( \frac{dy}{dx} \bigg|_{x=\frac{\pi}{2}} = -1 \) has

(A) no solution \hspace{1cm} (B) exactly two solutions

(C) exactly one solution \hspace{1cm} (D) infinitely many solutions

Correct : 1  Wrong : -0.33
Question Number : 5  
Correct : 1  Wrong : 0

A six-face fair dice is rolled a large number of times. The mean value of the outcomes is ________

Question Number : 6  
Correct : 1  Wrong : -0.33

For steady flow of a viscous incompressible fluid through a circular pipe of constant diameter, the average velocity in the fully developed region is constant. Which one of the following statements about the average velocity in the developing region is TRUE?

(A) It increases until the flow is fully developed.
(B) It is constant and is equal to the average velocity in the fully developed region.
(C) It decreases until the flow is fully developed.
(D) It is constant but is always lower than the average velocity in the fully developed region.

Question Number : 7  
Correct : 1  Wrong : -0.33

Consider the two-dimensional velocity field given by \( \vec{V} = (5 + a_1 x + b_1 y) \hat{i} + (4 + a_2 x + b_2 y) \hat{j} \), where \( a_1, b_1, a_2 \) and \( b_2 \) are constants. Which one of the following conditions needs to be satisfied for the flow to be incompressible?

(A) \( a_1 + b_1 = 0 \)  
(B) \( a_1 + b_2 = 0 \)
(C) \( a_2 + b_2 = 0 \)  
(D) \( a_2 + b_1 = 0 \)

Question Number : 8  
Correct : 1  Wrong : 0

Water (density = 1000 kg/m\(^3\)) at ambient temperature flows through a horizontal pipe of uniform cross section at the rate of 1 kg/s. If the pressure drop across the pipe is 100 kPa, the minimum power required to pump the water across the pipe, in watts, is ________

Question Number : 9  
Correct : 1  Wrong : -0.33

Which one of the following is NOT a rotating machine?

(A) Centrifugal pump  
(B) Gear pump
(C) Jet pump  
(D) Vane pump
Question Number : 10

Saturated steam at 100°C condenses on the outside of a tube. Cold fluid enters the tube at 20 °C and exits at 50 °C. The value of the Log Mean Temperature Difference (LMTD) is \( \)°C.

Question Number : 11

The molar specific heat at constant volume of an ideal gas is equal to 2.5 times the universal gas constant \((8.314 \text{ J/mol·K})\). When the temperature increases by 100 K, the change in molar specific enthalpy is \( \) J/mol.

Question Number : 12

A heat pump absorbs 10 kW of heat from outside environment at 250 K while absorbing 15 kW of work. It delivers the heat to a room that must be kept warm at 300 K. The Coefficient of Performance (COP) of the heat pump is \( \)

Question Number : 13

The Poisson’s ratio for a perfectly incompressible linear elastic material is

(A) 1    (B) 0.5    (C) 0    (D) infinity

Question Number : 14

A particle of unit mass is moving on a plane. Its trajectory, in polar coordinates, is given by \( r(t) = t^2, \theta(t) = t \), where \( t \) is time. The kinetic energy of the particle at time \( t = 2 \) is

(A) 4    (B) 12    (C) 16    (D) 24

Question Number : 15

A motor driving a solid circular steel shaft transmits 40 kW of power at 500 rpm. If the diameter of the shaft is 40 mm, the maximum shear stress in the shaft is \( \) MPa.
Question Number : 16  
Correct : 1  Wrong : -0.33

Consider a beam with circular cross-section of diameter \( d \). The ratio of the second moment of area about the neutral axis to the section modulus of the area is

(A) \( \frac{d}{2} \)  
(B) \( \frac{\pi d^2}{2} \)  
(C) \( d \)  
(D) \( \pi d \)

Question Number : 17  
Correct : 1  Wrong : 0

The following figure shows the velocity-time plot for a particle traveling along a straight line. The distance covered by the particle from \( t = 0 \) to \( t = 5 \) s is \( \underline{} \) m.

![Velocity-time plot](image)

Question Number : 18  
Correct : 1  Wrong : -0.33

The damping ratio for a viscously damped spring mass system, governed by the relationship \( m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx = F(t) \), is given by

(A) \( \frac{c}{\sqrt{mk}} \)  
(B) \( \frac{c}{2\sqrt{km}} \)  
(C) \( \frac{c}{\sqrt{km}} \)  
(D) \( \sqrt{\frac{c}{2mk}} \)
Question Number : 19  
Correct : 1  Wrong : -0.33

Consider the schematic of a riveted lap joint subjected to tensile load $F$, as shown below. Let $d$ be the diameter of the rivets, and $S_f$ be the maximum permissible tensile stress in the plates. What should be the minimum value for the thickness of the plates to guard against tensile failure of the plates? Assume the plates to be identical.

![Diagram of riveted lap joint]

(A) $\frac{F}{S_f(W-2d)}$  
(B) $\frac{F}{S_f W}$  
(C) $\frac{F}{S_f W}$  
(D) $\frac{2F}{S_f W}$

Question Number : 20  
Correct : 1  Wrong : -0.33

Cylindrical pins of diameter $15 \pm 0.020$ mm are being produced on a machine. Statistical quality control tests show a mean of 14.995 mm and standard deviation of 0.004 mm. The process capability index $C_p$ is

(A) 0.833  
(B) 1.667  
(C) 3.333  
(D) 3.750

Question Number : 21  
Correct : 1  Wrong : 0

In a metal forming operation when the material has just started yielding, the principal stresses are $\sigma_1 = +180$ MPa, $\sigma_2 = -100$ MPa, $\sigma_3 = 0$. Following von Mises’ criterion, the yield stress is ______________ MPa.
**Question Number : 22**

Match the processes with their characteristics.

<table>
<thead>
<tr>
<th>Process</th>
<th>Characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>P: Electrical Discharge Machining</td>
<td>1. No residual stress</td>
</tr>
<tr>
<td>Q: Ultrasonic machining</td>
<td>2. Machining of electrically conductive materials</td>
</tr>
<tr>
<td>R: Chemical machining</td>
<td>3. Machining of glass</td>
</tr>
<tr>
<td>S: Ion Beam Machining</td>
<td>4. Nano-machining</td>
</tr>
</tbody>
</table>

(A) P-2, Q-3, R-1, S-4  
(B) P-3, Q-2, R-1, S-4  
(C) P-3, Q-2, R-4, S-1  
(D) P-2, Q-4, R-3, S-1

**Question Number : 23**

In an arc welding process, welding speed is doubled. Assuming all other process parameters to be constant, the cross sectional area of the weld bead will

(A) increase by 25 %  
(B) increase by 50 %  
(C) reduce by 25 %  
(D) reduce by 50 %

**Question Number : 24**

Metric thread of 0.8 mm pitch is to be cut on a lathe. Pitch of the lead screw is 1.5 mm. If the spindle rotates at 1500 rpm, the speed of rotation of the lead screw (rpm) will be __________

**Question Number : 25**

In the engineering stress-strain curve for mild steel, the Ultimate Tensile Strength (UTS) refers to

(A) Yield stress  
(B) Proportional limit  
(C) Maximum stress  
(D) Fracture stress
Consider the matrix \( P = \begin{bmatrix} \frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ 0 & 1 & 0 \\ -\frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \end{bmatrix} \).

Which one of the following statements about \( P \) is INCORRECT?

(A) Determinant of \( P \) is equal to 1.
(B) \( P \) is orthogonal.
(C) Inverse of \( P \) is equal to its transpose.
(D) All eigenvalues of \( P \) are real numbers.

For the vector \( \vec{V} = 2yz \hat{i} + 3xz \hat{j} + 4xy \hat{k} \), the value of \( \nabla \times \vec{V} \) is ____________

A parametric curve defined by \( x = \cos \left( \frac{\pi u}{2} \right) \), \( y = \sin \left( \frac{\pi u}{2} \right) \) in the range \( 0 \leq u \leq 1 \) is rotated about the X-axis by 360 degrees. Area of the surface generated is

(A) \( \frac{\pi}{2} \)  
(B) \( \pi \)  
(C) 2\( \pi \)  
(D) 4\( \pi \)

P (0, 3), Q (0.5, 4), and R (1, 5) are three points on the curve defined by \( f(x) \). Numerical integration is carried out using both Trapezoidal rule and Simpson’s rule within limits \( x = 0 \) and \( x = 1 \) for the curve. The difference between the two results will be

(A) 0  
(B) 0.25  
(C) 0.5  
(D) 1
Question Number : 30  
Correct : 2  Wrong : -0.66

The velocity profile inside the boundary layer for flow over a flat plate is given as \( \frac{u}{U_\infty} = \sin \left( \frac{\pi y}{2 \delta} \right) \), where \( U_\infty \) is the free stream velocity and \( \delta \) is the local boundary layer thickness. If \( \delta^* \) is the local displacement thickness, the value of \( \frac{\delta^*}{\delta} \) is

(A) \( \frac{2}{\pi} \)  \hspace{1cm} (B) \( 1 - \frac{2}{\pi} \)  \hspace{1cm} (C) \( 1 + \frac{2}{\pi} \)  \hspace{1cm} (D) 0

Question Number : 31  
Correct : 2  Wrong : -0.66

Consider steady flow of an incompressible fluid through two long and straight pipes of diameters \( d_1 \) and \( d_2 \) arranged in series. Both pipes are of equal length and the flow is turbulent in both pipes. The friction factor for turbulent flow through pipes is of the form, \( f = K(Re)^{-n} \), where \( K \) and \( n \) are known positive constants and \( Re \) is the Reynolds number. Neglecting minor losses, the ratio of the frictional pressure drop in pipe 1 to that in pipe 2, \( \frac{\Delta P_1}{\Delta P_2} \), is given by

(A) \( \left( \frac{d_2}{d_1} \right)^{(5-n)} \)  \hspace{1cm} (B) \( \left( \frac{d_2}{d_1} \right)^5 \)  \hspace{1cm} (C) \( \left( \frac{d_2}{d_1} \right)^{(3-n)} \)  \hspace{1cm} (D) \( \left( \frac{d_2}{d_1} \right)^{(5+n)} \)

Question Number : 32  
Correct : 2  Wrong : -0.66

For a steady flow, the velocity field is \( \vec{V} = (-x^2 + 3y)i + (2xy)j \). The magnitude of the acceleration of a particle at \((1, -1)\) is

(A) 2  \hspace{1cm} (B) 1  \hspace{1cm} (C) \( 2\sqrt{5} \)  \hspace{1cm} (D) 0

Question Number : 33  
Correct : 2  Wrong : 0

One kg of an ideal gas (gas constant, \( R = 400 \) J/kg.K, specific heat at constant volume, \( c_v = 1000 \) J/kg.K) at 1 bar, and 300 K is contained in a sealed rigid cylinder. During an adiabatic process, 100 kJ of work is done on the system by a stirrer. The increase in entropy of the system is ______ J/K.

Question Number : 34  
Correct : 2  Wrong : 0

The pressure ratio across a gas turbine (for air, specific heat at constant pressure, \( c_p = 1040 \) J/kg.K and ratio of specific heats, \( \gamma = 1.4 \)) is 10. If the inlet temperature to the turbine is 1200 K and the isentropic efficiency is 0.9, the gas temperature at turbine exit is ________ K.
Question Number : 35  Correct : 2  Wrong : 0

Moist air is treated as an ideal gas mixture of water vapor and dry air (molecular weight of air = 28.84 and molecular weight of water = 18). At a location, the total pressure is 100 kPa, the temperature is 30 °C and the relative humidity is 55%. Given that the saturation pressure of water at 30 °C is 4246 Pa, the mass of water vapor per kg of dry air is ________________ grams.

Question Number : 36  Correct : 2  Wrong : 0

Air contains 79% N₂ and 21% O₂ on a molar basis. Methane (CH₄) is burned with 50% excess air than required stoichiometrically. Assuming complete combustion of methane, the molar percentage of N₂ in the products is ________________

Question Number : 37  Correct : 2  Wrong : 0

Two black surfaces, AB and BC, of lengths 5 m and 6 m, respectively, are oriented as shown. Both surfaces extend infinitely into the third dimension. Given that view factor \( F_{12} = 0.5 \), \( T_1 = 800 \text{K} \), \( T_2 = 600 \text{K} \), \( T_{\text{surrounding}} = 300 \text{K} \) and Stefan Boltzmann constant, \( \sigma = 5.67 \times 10^{-8} \text{W/(m}^2\text{K}^4) \), the heat transfer rate from Surface 2 to the surrounding environment is __________kW.
Question Number : 38
Correct : 2  Wrong : 0

Heat is generated uniformly in a long solid cylindrical rod (diameter = 10 mm) at the rate of $4 \times 10^7$ W/m$^3$. The thermal conductivity of the rod material is 25 W/m.K. Under steady state conditions, the temperature difference between the centre and the surface of the rod is ______°C.

Question Number : 39
Correct : 2  Wrong : -0.66

An initially stress-free massless elastic beam of length $L$ and circular cross-section with diameter $d$ ($d \ll L$) is held fixed between two walls as shown. The beam material has Young’s modulus $E$ and coefficient of thermal expansion $\alpha$.

![Beam Diagram]

If the beam is slowly and uniformly heated, the temperature rise required to cause the beam to buckle is proportional to

(A) $d$  (B) $d^2$  (C) $d^3$  (D) $d^4$

Question Number : 40
Correct : 2  Wrong : 0

A point mass of 100 kg is dropped onto a massless elastic bar (cross-sectional area = 100 mm$^2$, length = 1 m, Young’s modulus = 100 GPa) from a height $H$ of 10 mm as shown (Figure is not to scale). If $g = 10$ m/s$^2$, the maximum compression of the elastic bar is ____ mm.

![Mass on Elastic Bar Diagram]
Question Number : 41  Correct : 2  Wrong : -0.66

Two disks A and B with identical mass \((m)\) and radius \((R)\) are initially at rest. They roll down from the top of identical inclined planes without slipping. Disk A has all of its mass concentrated at the rim, while Disk B has its mass uniformly distributed. At the bottom of the plane, the ratio of velocity of the center of disk A to the velocity of the center of disk B is

\[
(A) \frac{\sqrt{3}}{4} \quad (B) \frac{\sqrt{3}}{2} \quad (C) 1 \quad (D) \sqrt{2}
\]

Question Number : 42  Correct : 2  Wrong : 0

A rectangular region in a solid is in a state of plane strain. The \((x,y)\) coordinates of the corners of the undeformed rectangle are given by \(P(0,0), Q(4,0), R(4,3), S(0,3)\). The rectangle is subjected to uniform strains, \(\varepsilon_{xx} = 0.001, \varepsilon_{yy} = 0.002, \gamma_{xy} = 0.003\). The deformed length of the elongated diagonal, \(\text{upto three decimal places}\), is \(\text{units}\).

Question Number : 43  Correct : 2  Wrong : 0

A machine element has an ultimate strength \((\sigma_u)\) of 600 N/mm\(^2\), and endurance limit \((\sigma_{en})\) of 250 N/mm\(^2\). The fatigue curve for the element on a \textbf{log-log} plot is shown below. If the element is to be designed for a finite life of 10,000 cycles, the maximum amplitude of a completely reversed operating stress is \(\text{N/mm}\(^2\).\)
Question Number : 44

A horizontal bar, fixed at one end \((x = 0)\), has a length of 1 m, and cross-sectional area of 100 mm\(^2\). Its elastic modulus varies along its length as given by \(E(x) = 100 \, e^{-x} \) GPa, where \(x\) is the length coordinate (in m) along the axis of the bar. An axial tensile load of 10 kN is applied at the free end \((x = 1)\). The axial displacement of the free end is ______ mm.

Question Number : 45

In an epicyclic gear train, shown in the figure, the outer ring gear is fixed, while the sun gear rotates counterclockwise at 100 rpm. Let the number of teeth on the sun, planet and outer gears to be 50, 25, and 100, respectively. The ratio of magnitudes of angular velocity of the planet gear to the angular velocity of the carrier arm is ________.
A thin uniform rigid bar of length \( L \) and mass \( M \) is hinged at point \( O \), located at a distance of \( \frac{L}{3} \) from one of its ends. The bar is further supported using springs, each of stiffness \( k \), located at the two ends. A particle of mass \( m = \frac{M}{4} \) is fixed at one end of the bar, as shown in the figure. For small rotations of the bar about \( O \), the natural frequency of the system is

\[
\begin{align*}
\text{(A)} & \quad \sqrt{\frac{5k}{M}} \\
\text{(B)} & \quad \sqrt{\frac{5k}{2M}} \\
\text{(C)} & \quad \sqrt{\frac{3k}{2M}} \\
\text{(D)} & \quad \sqrt{\frac{3k}{M}}
\end{align*}
\]

**Question Number : 47**

For an inline slider-crank mechanism, the lengths of the crank and connecting rod are 3 m and 4 m, respectively. At the instant when the connecting rod is perpendicular to the crank, if the velocity of the slider is 1 m/s, the magnitude of angular velocity (upto 3 decimal points accuracy) of the crank is \__________ radian/s.

**Question Number : 48**

A 10 mm deep cylindrical cup with diameter of 15 mm is drawn from a circular blank. Neglecting the variation in the sheet thickness, the diameter (upto 2 decimal points accuracy) of the blank is \__________ mm.
Question Number : 49  Correct : 2  Wrong : -0.66

Circular arc on a part profile is being machined on a vertical CNC milling machine. CNC part program using metric units with absolute dimensions is listed below:

```
N60 G01 X 30 Y 55 Z -5 F50
N70 G02 X 50 Y 35 R 20
N80 G01 Z 5
```

The coordinates of the centre of the circular arc are:

(A) (30, 55)        (B) (50, 55)        (C) (50, 35)        (D) (30, 35)

Question Number : 50  Correct : 2  Wrong : -0.66

Assume that the surface roughness profile is triangular as shown schematically in the figure. If the peak to valley height is 20 μm, the central line average surface roughness Rₐ (in μm) is

![Triangular Surface Roughness Profile]

(A) 5        (B) 6.67        (C) 10        (D) 20

Question Number : 51  Correct : 2  Wrong : 0

Two models, P and Q, of a product earn profits of Rs. 100 and Rs. 80 per piece, respectively. Production times for P and Q are 5 hours and 3 hours, respectively, while the total production time available is 150 hours. For a total batch size of 40, to maximize profit, the number of units of P to be produced is __________

Question Number : 52  Correct : 2  Wrong : 0

Following data refers to the jobs (P, Q, R, S) which have arrived at a machine for scheduling. The shortest possible average flow time is __________ days.

<table>
<thead>
<tr>
<th>Job</th>
<th>Processing Time (days)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>15</td>
</tr>
<tr>
<td>Q</td>
<td>9</td>
</tr>
<tr>
<td>R</td>
<td>22</td>
</tr>
<tr>
<td>S</td>
<td>12</td>
</tr>
</tbody>
</table>
Question Number : 53  
Correct : 2  Wrong : 0

A block of length 200 mm is machined by a slab milling cutter 34 mm in diameter. The depth of cut and table feed are set at 2 mm and 18 mm/minute, respectively. Considering the approach and the over travel of the cutter to be same, the minimum estimated machining time per pass is _________ minutes.

Question Number : 54  
Correct : 2  Wrong : 0

A sprue in a sand mould has a top diameter of 20 mm and height of 200 mm. The velocity of the molten metal at the entry of the sprue is 0.5 m/s. Assume acceleration due to gravity as 9.8 m/s² and neglect all losses. If the mould is well ventilated, the velocity (upto 3 decimal points accuracy) of the molten metal at the bottom of the sprue is _________ m/s.

Question Number : 55  
Correct : 2  Wrong : 0

Two cutting tools with tool life equations given below are being compared:

Tool 1: \( V^0.1 = 150 \)
Tool 2: \( V^0.3 = 300 \)

where \( V \) is cutting speed in m/minute and \( T \) is tool life in minutes. The breakeven cutting speed beyond which Tool 2 will have a higher tool life is _______ m/minute.
Question Number : 56
Correct : 1 Wrong : -0.33

He was one of my best ________ and I felt his loss ________.
(A) friend, keenly  (B) friends, keen  (C) friend, keener  (D) friends, keenly

Question Number : 57
Correct : 1 Wrong : -0.33

As the two speakers became increasingly agitated, the debate became ________.
(A) lukewarm  (B) poetic  (C) forgiving  (D) heated

Question Number : 58
Correct : 1 Wrong : -0.33

A right-angled cone (with base radius 5 cm and height 12 cm), as shown in the figure below, is rolled on the ground keeping the point P fixed until the point Q (at the base of the cone, as shown) touches the ground again.

By what angle (in radians) about P does the cone travel?

(A) $\frac{5\pi}{12}$  (B) $\frac{5\pi}{24}$  (C) $\frac{24\pi}{5}$  (D) $\frac{10\pi}{13}$

Question Number : 59
Correct : 1 Wrong : -0.33

In a company with 100 employees, 45 earn Rs. 20,000 per month, 25 earn Rs. 30,000, 20 earn Rs. 40,000, 8 earn Rs. 60,000, and 2 earn Rs. 150,000. The median of the salaries is

(A) Rs. 20,000  (B) Rs. 30,000  (C) Rs. 32,300  (D) Rs. 40,000
Question Number : 60
Correct : 1 Wrong : -0.33

P, Q, and R talk about S's car collection. P states that S has at least 3 cars. Q believes that S has less than 3 cars. R indicates that to his knowledge, S has at least one car. Only one of P, Q and R is right. The number of cars owned by S is

(A) 0  (B) 1  (C) 3  (D) Cannot be determined

Question Number : 61
Correct : 2 Wrong : -0.66

“Here, throughout the early 1820s, Stuart continued to fight his losing battle to allow his sepoys to wear their caste-marks and their own choice of facial hair on parade, being again reprimanded by the commander-in-chief. His retort that ‘A stronger instance than this of European prejudice with relation to this country has never come under my observations’ had no effect on his superiors.”

According to this paragraph, which of the statements below is most accurate?

(A) Stuart’s commander-in-chief was moved by this demonstration of his prejudice.
(B) The Europeans were accommodating of the sepoys’ desire to wear their caste-marks.
(C) Stuart’s ‘losing battle’ refers to his inability to succeed in enabling sepoys to wear caste-marks.
(D) The commander-in-chief was exempt from the European prejudice that dictated how the sepoys were to dress.

Question Number : 62
Correct : 2 Wrong : -0.66

What is the sum of the missing digits in the subtraction problem below?

\[
\begin{array}{c}
\phantom{5}\phantom{4}8\phantom{8}9 \\
\hline
1\phantom{1}1\phantom{1}1 \\
\end{array}
\]

(A) 8  (B) 10  (C) 11  (D) Cannot be determined

Question Number : 63
Correct : 2 Wrong : -0.66

Let \( S_1 \) be the plane figure consisting of the points \((x, y)\) given by the inequalities \(|x - 1| \leq 2\) and \(|y + 2| \leq 3\). Let \( S_2 \) be the plane figure given by the inequalities \(x - y \geq -2\), \(y \geq 1\), and \(x \leq 3\). Let \( S \) be the union of \( S_1 \) and \( S_2 \). The area of \( S \) is

(A) 26  (B) 28  (C) 32  (D) 34
Two very famous sportsmen Mark and Steve happened to be brothers, and played for country K. Mark teased James, an opponent from country E. “There is no way you are good enough to play for your country.” James replied, “Maybe not, but at least I am the best player in my own family.”

Which one of the following can be inferred from this conversation?

(A) Mark was known to play better than James
(B) Steve was known to play better than Mark
(C) James and Steve were good friends
(D) James played better than Steve

The growth of bacteria (lactobacillus) in milk leads to curd formation. A minimum bacterial population density of 0.8 (in suitable units) is needed to form curd. In the graph below, the population density of lactobacillus in 1 litre of milk is plotted as a function of time, at two different temperatures, 25 °C and 37 °C.

Consider the following statements based on the data shown above:

1. The growth in bacterial population stops earlier at 37 °C as compared to 25 °C
2. The time taken for curd formation at 25 °C is twice the time taken at 37 °C

Which one of the following options is correct?

(A) Only i  (B) Only ii  (C) Both i and ii  (D) Neither i nor ii
Graduate Aptitude Test in Engineering 2017

Question Paper Name: Mechanical Engineering 4th feb 2017 session 2
Subject Name: Mechanical Engineering
Duration: 180
Total Marks: 100

Organizing Institute:
Indian Institute of Technology Roorkee
Question Number : 1  Correct : 1  Wrong : 0
Two coins are tossed simultaneously. The probability (upto two decimal points accuracy) of getting at least one head is__________

Question Number : 2  Correct : 1  Wrong : 0
The divergence of the vector \(-yi + xj\) is__________

Question Number : 3  Correct : 1  Wrong : 0
The determinant of a 2x2 matrix is 50. If one eigenvalue of the matrix is 10, the other eigenvalue is__________

Question Number : 4  Correct : 1  Wrong : -0.33
A sample of 15 data is as follows: 17, 18, 17, 17, 13, 18, 5, 5, 6, 7, 8, 9, 20, 17, 3. The mode of the data is
(A) 4  (B) 13  (C) 17  (D) 20

Question Number : 5  Correct : 1  Wrong : -0.33
The Laplace transform of \(te^t\) is
(A) \(\frac{s}{(s+1)^2}\)  (B) \(\frac{1}{(s-1)^2}\)  (C) \(\frac{1}{(s+1)^2}\)  (D) \(\frac{s}{s-1}\)
Question Number : 6  Correct : 1  Wrong : -0.33

A mass $m$ is attached to two identical springs having spring constant $k$ as shown in the figure. The natural frequency $\omega$ of this single degree of freedom system is

\[ \omega = \sqrt{\frac{2k}{m}} \]

Question Number : 7  Correct : 1  Wrong : 0

The state of stress at a point is $\sigma_x = \sigma_y = 0$, $\tau_{xz} = \tau_{zx} = \tau_{yz} = \tau_{zy} = 0$ and $\tau_{xy} = \tau_{yx} = 50 \text{ MPa}$. The maximum normal stress (in MPa) at that point is

Question Number : 8  Correct : 1  Wrong : 0

For a loaded cantilever beam of uniform cross-section, the bending moment (in N·mm) along the length is $M(x) = 5x^2 + 10x$, where $x$ is the distance (in mm) measured from the free end of the beam. The magnitude of shear force (in N) in the cross-section at $x = 10 \text{ mm}$ is

Question Number : 9  Correct : 1  Wrong : -0.33

A cantilever beam of length $L$ and flexural modulus $EI$ is subjected to a point load $P$ at the free end. The elastic strain energy stored in the beam due to bending (neglecting transverse shear) is

\[ (A) \frac{P^2L^3}{6EI} \quad (B) \frac{P^2L^3}{3EI} \quad (C) \frac{PL^3}{3EI} \quad (D) \frac{PL^3}{6EI} \]
Question Number : 10
Correct : 1  Wrong : 0

A steel bar is held by two fixed supports as shown in the figure and is subjected to an increase of temperature \( \Delta T = 100 \, ^\circ C \). If the coefficient of thermal expansion and Young’s modulus of elasticity of steel are \( 11 \times 10^{-6} / ^\circ C \) and 200 GPa, respectively, the magnitude of thermal stress (in MPa) induced in the bar is _________

![Diagram of steel bar held by two fixed supports](image)

Question Number : 11
Correct : 1  Wrong : 0

A machine component made of a ductile material is subjected to a variable loading with \( \sigma_{\min} = -50 \, \text{MPa} \) and \( \sigma_{\max} = 50 \, \text{MPa} \). If the corrected endurance limit and the yield strength for the material are \( \sigma'_{\text{e}} = 100 \, \text{MPa} \) and \( \sigma_{\text{y}} = 300 \, \text{MPa} \), respectively, the factor of safety is _________

Question Number : 12
Correct : 1  Wrong : 0

In a slider-crank mechanism, the lengths of the crank and the connecting rod are 100 mm and 160 mm, respectively. The crank is rotating with an angular velocity of 10 radian/s counterclockwise. The magnitude of linear velocity (in m/s) of the piston at the instant corresponding to the configuration shown in the figure is _________

![Diagram of slider-crank mechanism with dimensions](image)
Question Number : 13
Correct : 1 Wrong : -0.33
Which one of the following statements is **TRUE**?

(A) Both Pelton and Francis turbines are impulse turbines.
(B) Francis turbine is a reaction turbine but Kaplan turbine is an impulse turbine.
(C) Francis turbine is an axial-flow reaction turbine.
(D) Kaplan turbine is an axial-flow reaction turbine.

Question Number : 14
Correct : 1 Wrong : -0.33
A mass $m$ of a perfect gas at pressure $p_1$ and volume $V_1$ undergoes an isothermal process. The final pressure is $p_2$ and volume is $V_2$. The work done on the system is considered positive. If $R$ is the gas constant and $T$ is the temperature, then the work done in the process is

$(A) \quad p_1 V_1 \ln \frac{V_2}{V_1}$  \hspace{1cm}  $(B) \quad -p_1 V_1 \ln \frac{p_1}{p_2}$  \hspace{1cm}  $(C) \quad RT \ln \frac{V_2}{V_1}$  \hspace{1cm}  $(D) \quad -mRT \ln \frac{p_2}{p_1}$

Question Number : 15
Correct : 1 Wrong : -0.33
If a mass of moist air contained in a closed metallic vessel is heated, then its

(A) relative humidity decreases  \hspace{1cm}  (B) relative humidity increases
(C) specific humidity increases  \hspace{1cm}  (D) specific humidity decreases

Question Number : 16
Correct : 1 Wrong : -0.33
For the stability of a floating body the

(A) centre of buoyancy must coincide with the centre of gravity
(B) centre of buoyancy must be above the centre of gravity
(C) centre of gravity must be above the centre of buoyancy
(D) metacentre must be above the centre of gravity
Question Number : 17  Correct : 1 Wrong : -0.33

Consider a laminar flow at zero incidence over a flat plate. The shear stress at the wall is denoted by $\tau_w$. The axial positions $x_1$ and $x_2$ on the plate are measured from the leading edge in the direction of flow. If $x_2 > x_1$, then

(A) $\tau_w|_{x_1} = \tau_w|_{x_2} = 0$
(B) $\tau_w|_{x_1} = \tau_w|_{x_2} \neq 0$
(C) $\tau_w|_{x_1} > \tau_w|_{x_2}$
(D) $\tau_w|_{x_1} < \tau_w|_{x_2}$

Question Number : 18  Correct : 1 Wrong : 0

The heat loss from a fin is 6 W. The effectiveness and efficiency of the fin are 3 and 0.75, respectively. The heat loss (in W) from the fin, keeping the entire fin surface at base temperature, is ________

Question Number : 19  Correct : 1 Wrong : -0.33

The emissive power of a blackbody is $P$. If its absolute temperature is doubled, the emissive power becomes

(A) $2P$
(B) $4P$
(C) $8P$
(D) $16P$

Question Number : 20  Correct : 1 Wrong : -0.33

Which one of the following statements is **TRUE** for the ultrasonic machining (USM) process?

(A) In USM, the tool vibrates at subsonic frequency.
(B) USM does not employ magnetostrictive transducer.
(C) USM is an excellent process for machining ductile materials.
(D) USM often uses a slurry comprising abrasive-particles and water.

Question Number : 21  Correct : 1 Wrong : -0.33

The crystal structure of aluminium is

(A) body-centred cubic
(B) face-centred cubic
(C) close-packed hexagonal
(D) body-centred tetragonal
Question Number : 22  Correct : 1  Wrong : 0
Given the atomic weight of Fe is 56 and that of C is 12, the weight percentage of carbon in cementite (Fe₃C) is__________

Question Number : 23  Correct : 1  Wrong : -0.33
For a single server with Poisson arrival and exponential service time, the arrival rate is 12 per hour. Which one of the following service rates will provide a steady state finite queue length?
(A) 6 per hour   (B) 10 per hour   (C) 12 per hour   (D) 24 per hour

Question Number : 24  Correct : 1  Wrong : 0
The standard deviation of linear dimensions P and Q are 3 µm and 4 µm, respectively. When assembled, the standard deviation (in µm) of the resulting linear dimension (P+Q) is__________

Question Number : 25  Correct : 1  Wrong : -0.33
It is desired to make a product having T-shaped cross-section from a rectangular aluminium block. Which one of the following processes is expected to provide the highest strength of the product?
(A) Welding   (B) Casting   (C) Metal forming   (D) Machining

Question Number : 26  Correct : 2  Wrong : 0
The surface integral \( \iint_{S} \mathbf{F} \cdot \mathbf{n} \, dS \) over the surface \( S \) of the sphere \( x^2 + y^2 + z^2 = 9 \), where \( \mathbf{F} = (x+y)\mathbf{i} + (x+z)\mathbf{j} + (y+z)\mathbf{k} \) and \( \mathbf{n} \) is the unit outward surface normal, yields__________
Consider the differential equation $3y''(x) + 27y(x) = 0$ with initial conditions $y(0) = 0$ and $y'(0) = 2000$. The value of $y$ at $x = 1$ is__________

**Question Number : 28**

Consider the matrix $A = \begin{bmatrix} 50 & 70 \\ 70 & 80 \end{bmatrix}$ whose eigenvectors corresponding to eigenvalues $\lambda_1$ and $\lambda_2$ are $x_1 = \begin{bmatrix} 70 \\ \lambda_1 - 50 \end{bmatrix}$ and $x_2 = \begin{bmatrix} \lambda_2 - 80 \\ 70 \end{bmatrix}$, respectively. The value of $x_1^T x_2$ is__________

**Question Number : 29**

If $f(z) = (x^2 + ay^2) + ibxy$ is a complex analytic function of $z = x + iy$, where $i = \sqrt{-1}$, then

(A) $a = -1, b = -1$  
(B) $a = -1, b = 2$  
(C) $a = 1, b = 2$  
(D) $a = 2, b = 2$

**Question Number : 30**

Block 2 slides outward on link 1 at a uniform velocity of 6 m/s as shown in the figure. Link 1 is rotating at a constant angular velocity of 20 radian/s counterclockwise. The magnitude of the total acceleration (in m/s²) of point P of the block with respect to fixed point O is__________
The radius of gyration of a compound pendulum about the point of suspension is 100 mm. The distance between the point of suspension and the centre of mass is 250 mm. Considering the acceleration due to gravity as 9.81 m/s², the natural frequency (in radian/s) of the compound pendulum is__________

A gear train shown in the figure consists of gears P, Q, R and S. Gear Q and gear R are mounted on the same shaft. All the gears are mounted on parallel shafts and the number of teeth of P, Q, R and S are 24, 45, 30 and 80, respectively. Gear P is rotating at 400 rpm. The speed (in rpm) of the gear S is__________

A helical compression spring made of a wire of circular cross-section is subjected to a compressive load. The maximum shear stress induced in the cross-section of the wire is 24 MPa. For the same compressive load, if both the wire diameter and the mean coil diameter are doubled, the maximum shear stress (in MPa) induced in the cross-section of the wire is__________
Question Number : 34

Three masses are connected to a rotating shaft supported on bearings A and B as shown in the figure. The system is in a space where the gravitational effect is absent. Neglect the mass of shaft and rods connecting the masses. For $m_1 = 10$ kg, $m_2 = 5$ kg and $m_3 = 2.5$ kg and for a shaft angular speed of 1000 radian/s, the magnitude of the bearing reaction (in N) at location B is___________

Question Number : 35

A steel plate, connected to a fixed channel using three identical bolts A, B and C, carries a load of 6 kN as shown in the figure. Considering the effect of direct load and moment, the magnitude of resultant shear force (in kN) on bolt C is

(A) 13
(B) 15
(C) 17
(D) 30
Question Number : 36

A single-plate clutch has a friction disc with inner and outer radii of 20 mm and 40 mm, respectively. The friction lining in the disc is made in such a way that the coefficient of friction $\mu$ varies radially as $\mu = 0.01r$, where $r$ is in mm. The clutch needs to transmit a friction torque of 18.85 kN·mm. As per uniform pressure theory, the pressure (in MPa) on the disc is__________

Question Number : 37

The principal stresses at a point in a critical section of a machine component are $\sigma_1 = 60$ MPa, $\sigma_2 = 5$ MPa and $\sigma_3 = -40$ MPa. For the material of the component, the tensile yield strength is $\sigma_y = 200$ MPa. According to the maximum shear stress theory, the factor of safety is

(A) 1.67  (B) 2.00  (C) 3.60  (D) 4.00

Question Number : 38

The rod PQ of length $L = \sqrt{2}$ m and uniformly distributed mass of $M = 10$ kg, is released from rest at the position shown in the figure. The ends slide along the frictionless faces OP and OQ. Assume acceleration due to gravity, $g = 10$ m/s$^2$. The mass moment of inertia of the rod about its centre of mass and an axis perpendicular to the plane of the figure is $(ML^2/12)$. At this instant, the magnitude of angular acceleration (in radian/s$^2$) of the rod is ____________
Question Number : 39  
Correct : 2  Wrong : 0

The arrangement shown in the figure measures the velocity $V$ of a gas of density $1 \text{ kg/m}^3$ flowing through a pipe. The acceleration due to gravity is $9.81 \text{ m/s}^2$. If the manometric fluid is water (density $1000 \text{ kg/m}^3$) and the velocity $V$ is $20 \text{ m/s}$, the differential head $h$ (in mm) between the two arms of the manometer is ____________.

![Diagram](Image)

Question Number : 40  
Correct : 2  Wrong : 0

A $60 \text{ mm}$-diameter water jet strikes a plate containing a hole of $40 \text{ mm}$ diameter as shown in the figure. Part of the jet passes through the hole horizontally, and the remaining is deflected vertically. The density of water is $1000 \text{ kg/m}^3$. If velocities are as indicated in the figure, the magnitude of horizontal force (in N) required to hold the plate is ____________.

![Diagram](Image)
Question Number : 41
Correct : 2  Wrong : 0
For the laminar flow of water over a sphere, the drag coefficient \( C_F \) is defined as
\[
C_F = \frac{F}{\rho U^2 D^2},
\]
where \( F \) is the drag force, \( \rho \) is the fluid density, \( U \) is the fluid velocity and \( D \) is the diameter of the sphere. The density of water is 1000 kg/m\(^3\). When the diameter of the sphere is 100 mm and the fluid velocity is 2 m/s, the drag coefficient is 0.5. If water now flows over another sphere of diameter 200 mm under dynamically similar conditions, the drag force (in N) on this sphere is__________

Question Number : 42
Correct : 2  Wrong : 0
In the Rankine cycle for a steam power plant the turbine entry and exit enthalpies are 2803 kJ/kg and 1800 kJ/kg, respectively. The enthalpies of water at pump entry and exit are 121 kJ/kg and 124 kJ/kg, respectively. The specific steam consumption (in kg/kW.h) of the cycle is__________

Question Number : 43
Correct : 2  Wrong : -0.66
A calorically perfect gas (specific heat at constant pressure 1000 J/kg·K) enters and leaves a gas turbine with the same velocity. The temperatures of the gas at turbine entry and exit are 1100 K and 400 K, respectively. The power produced is 4.6 MW and heat escapes at the rate of 300 kJ/s through the turbine casing. The mass flow rate of the gas (in kg/s) through the turbine is

(A) 6.14  
(B) 7.00  
(C) 7.50  
(D) 8.00

Question Number : 44
Correct : 2  Wrong : 0
One kg of an ideal gas (gas constant \( R = 287 \) J/kg·K) undergoes an irreversible process from state-1 (1 bar, 300 K) to state-2 (2 bar, 300 K). The change in specific entropy \((s_2 - s_1)\) of the gas (in J/kg·K) in the process is__________
The volume and temperature of air (assumed to be an ideal gas) in a closed vessel is 2.87 m$^3$ and 300 K, respectively. The gauge pressure indicated by a manometer fitted to the wall of the vessel is 0.5 bar. If the gas constant of air is $R = 287$ J/kg·K and the atmospheric pressure is 1 bar, the mass of air (in kg) in the vessel is

(A) 1.67  (B) 3.33  (C) 5.00  (D) 6.66

In a counter-flow heat exchanger, water is heated at the rate of 1.5 kg/s from 40 °C to 80 °C by an oil entering at 120 °C and leaving at 60 °C. The specific heats of water and oil are 4.2 kJ/kg·K and 2 kJ/kg·K, respectively. The overall heat transfer coefficient is 400 W/m$^2$·K. The required heat transfer surface area (in m$^2$) is

(A) 0.104  (B) 0.022  (C) 10.4  (D) 21.84

A metal ball of diameter 60 mm is initially at 220 °C. The ball is suddenly cooled by an air jet of 20 °C. The heat transfer coefficient is 200 W/m$^2$·K. The specific heat, thermal conductivity and density of the metal ball are 400 J/kg·K, 400 W/m·K and 9000 kg/m$^3$, respectively. The ball temperature (in °C) after 90 seconds will be approximately

(A) 141  (B) 163  (C) 189  (D) 210

A product made in two factories, P and Q, is transported to two destinations, R and S. The per unit costs of transportation (in Rupees) from factories to destinations are as per the following matrix:

<table>
<thead>
<tr>
<th>Factory</th>
<th>Destination</th>
<th>R</th>
<th>S</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td></td>
<td>10</td>
<td>7</td>
</tr>
<tr>
<td>Q</td>
<td></td>
<td>3</td>
<td>4</td>
</tr>
</tbody>
</table>

Factory P produces 7 units and factory Q produces 9 units of the product. Each destination requires 8 units. If the north-west corner method provides the total transportation cost as $X$ (in Rupees) and the optimized (the minimum) total transportation cost is $Y$ (in Rupees), then ($X-Y$), in Rupees, is

(A) 0  (B) 15  (C) 35  (D) 105
**Question Number : 49**

A project starts with activity A and ends with activity F. The precedence relation and durations of the activities are as per the following table:

<table>
<thead>
<tr>
<th>Activity</th>
<th>Immediate predecessor</th>
<th>Duration (days)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>–</td>
<td>4</td>
</tr>
<tr>
<td>B</td>
<td>A</td>
<td>3</td>
</tr>
<tr>
<td>C</td>
<td>A</td>
<td>7</td>
</tr>
<tr>
<td>D</td>
<td>B</td>
<td>14</td>
</tr>
<tr>
<td>E</td>
<td>C</td>
<td>4</td>
</tr>
<tr>
<td>F</td>
<td>D, E</td>
<td>9</td>
</tr>
</tbody>
</table>

The minimum project completion time (in days) is__________

**Question Number : 50**

A rod of length 20 mm is stretched to make a rod of length 40 mm. Subsequently, it is compressed to make a rod of final length 10 mm. Consider the longitudinal tensile strain as positive and compressive strain as negative. The total true longitudinal strain in the rod is

(A) $-0.5$  
(B) $-0.69$  
(C) $-0.75$  
(D) $-1.0$

**Question Number : 51**

Maximize $Z = 5x_1 + 3x_2$,
subject to
$x_1 + 2x_2 \leq 10,$
$x_1 - x_2 \leq 8,$
$x_1, x_2 \geq 0.$

In the starting Simplex tableau, $x_1$ and $x_2$ are non-basic variables and the value of $Z$ is zero. The value of $Z$ in the next Simplex tableau is__________
Question Number : 52  Correct : 2  Wrong : 0

A strip of 120 mm width and 8 mm thickness is rolled between two 300 mm-diameter rolls to get a strip of 120 mm width and 7.2 mm thickness. The speed of the strip at the exit is 30 m/min. There is no front or back tension. Assuming uniform roll pressure of 200 MPa in the roll bite and 100% mechanical efficiency, the minimum total power (in kW) required to drive the two rolls is _________

Question Number : 53  Correct : 2  Wrong : 0

A cylindrical pin of $25^{+0.020}_{-0.020}$ mm diameter is electroplated. Plating thickness is $2.0^{+0.005}_{-0.010}$ mm. Neglecting the gauge tolerance, the diameter (in mm, up to 3 decimal points accuracy) of the GO ring gauge to inspect the plated pin is _________

Question Number : 54  Correct : 2  Wrong : -0.66

During the turning of a 20 mm-diameter steel bar at a spindle speed of 400 rpm, a tool life of 20 minute is obtained. When the same bar is turned at 200 rpm, the tool life becomes 60 minute. Assume that Taylor’s tool life equation is valid. When the bar is turned at 300 rpm, the tool life (in minute) is approximately

(A) 25  (B) 32  (C) 40  (D) 50

Question Number : 55  Correct : 2  Wrong : 0

In an orthogonal machining with a tool of $9^\circ$ orthogonal rake angle, the uncut chip thickness is 0.2 mm. The chip thickness fluctuates between 0.25 mm and 0.4 mm. The ratio of the maximum shear angle to the minimum shear angle during machining is _________
Question Number : 56  
Correct : 1  Wrong : -0.33

The ways in which this game can be played _______ potentially infinite.
(A) is  (B) is being  (C) are  (D) are being

Question Number : 57  
Correct : 1  Wrong : -0.33

If you choose plan P, you will have to _______ plan Q, as these two are mutually _______.
(A) forgo, exclusive  (B) forget, inclusive  (C) accept, exhaustive  (D) adopt, intrusive

Question Number : 58  
Correct : 1  Wrong : -0.33

If $a$ and $b$ are integers and $a - b$ is even, which of the following must always be even?
(A) $ab$  (B) $a^2 + b^2 + 1$  (C) $a^2 + b + 1$  (D) $ab - b$

Question Number : 59  
Correct : 1  Wrong : -0.33

A couple has 2 children. The probability that both children are boys if the older one is a boy is
(A) $1/4$  (B) $1/3$  (C) $1/2$  (D) 1

Question Number : 60  
Correct : 1  Wrong : -0.33

P looks at Q while Q looks at R. P is married, R is not. The number of pairs of people in which a married person is looking at an unmarried person is
(A) 0  (B) 1  (C) 2  (D) Cannot be determined
Question Number : 61
Correct : 2 Wrong : -0.66

“If you are looking for a history of India, or for an account of the rise and fall of the British Raj, or for the reason of the cleaving of the subcontinent into two mutually antagonistic parts and the effects this mutilation will have in the respective sections, and ultimately on Asia, you will not find it in these pages; for though I have spent a lifetime in the country, I lived too near the seat of events, and was too intimately associated with the actors, to get the perspective needed for the impartial recording of these matters.”

Which of the following is closest in meaning to ‘cleaving’?

(A) deteriorating  (B) arguing  (C) departing  (D) splitting

Question Number : 62
Correct : 2 Wrong : -0.66

X bullocks and Y tractors take 8 days to plough a field. If we halve the number of bullocks and double the number of tractors, it takes 5 days to plough the same field. How many days will it take X bullocks alone to plough the field?

(A) 30  (B) 35  (C) 40  (D) 45

Question Number : 63
Correct : 2 Wrong : -0.66

There are 4 women P, Q, R, S, and 5 men V, W, X, Y, Z in a group. We are required to form pairs each consisting of one woman and one man. P is not to be paired with Z, and Y must necessarily be paired with someone. In how many ways can 4 such pairs be formed?

(A) 74  (B) 76  (C) 78  (D) 80

Question Number : 64
Correct : 2 Wrong : -0.66

All people in a certain island are either ‘Knights’ or ‘Knaves’ and each person knows every other person’s identity. Knights NEVER lie, and knaves ALWAYS lie.

P says “Both of us are knights”. Q says “None of us are knaves”.

Which one of the following can be logically inferred from the above?

(A) Both P and Q are knights  
(B) P is a knight; Q is a knave  
(C) Both P and Q are knaves  
(D) The identities of P, Q cannot be determined
In the graph below, the concentration of a particular pollutant in a lake is plotted over (alternate) days of a month in winter (average temperature 10 °C) and a month in summer (average temperature 30 °C).

Consider the following statements based on the data shown above:

i. Over the given months, the difference between the maximum and the minimum pollutant concentrations is the same in both winter and summer.

ii. There are at least four days in the summer month such that the pollutant concentrations on those days are within 1 ppm of the pollutant concentrations on the corresponding days in the winter month.

Which one of the following options is correct?

(A) Only i  
(B) Only ii  
(C) Both i and ii  
(D) Neither i nor ii